# Algorithmic Composition, illustrated by my own work: A review of the period 1971-2008

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Since 1971, marking my first departure from fourteen years of spontaneous composition, my work has been mainly algorithmic in nature. Some of it was generated by single algorithm sets developed for multiple use, the properties of the results deriving from the input. In other cases, the algorithms were used once only, with the dedicated purpose of generating a single work. The algorithms ranged from verbal instructions to complex computer programs.

Of the eighty-odd pieces I have composed since 1971, about a quarter arose from three verbal scores, *Textmusic* (converting written text into notes), ...until... (working systematically with interval ratios) and *Relationships* (working with levels of complexity of melody and rhythm in the context of harmony and meter). Another quarter of the pieces were generated by three individual computer programs - *TXMS* (*Textmusic* packaged into software), *Autobusk* (for the generation of MIDI pitch sequences from scales and meters as well as twelve real-time variable parameters such as tonal and metric field strength) and *PAPAGEI* (for the generation of MIDI events based on patchable live interaction with an improvising performer). Yet another quarter of my compositions since 1971 have resulted from dedicated sets of algorithms for one-time use. Further computer programs such as *Synthrumentator* and *Spectasizer* (for the conversion of speech sounds into instrumental scores) were used to generate parts of other compositions.

In this paper I will refer to TXMS, Autobusk and Synthrumentator as well as to two compositions generated by dedicated software, ... or a cherish'd bard... (in which the algorithms generate all aspects of the piece from pitch and rhythm to the overall form) and Approximating Pi (in which algebraically defined algorithms generate the sound waves).

#### **Textmusic**

In 1970, the music I composed derived strongly from serial techniques of composers from Schoenberg to Stockhausen, dependent on music tradition and evolution. While doing so, I paused to consider whether it was possible to make music using concepts exclusively from everyday life. The result was *Textmusic* of April 1971, instructions for making a piano piece. Based on the orthography of a completely arbitrary text, I structured the linguistic concepts letters, syllables, words, phrases and sentences, the key-colors black/white/mixed as well as the physical traits loud/soft, short/long and (right pedal-) depressed/released:

Take a text consisting of a number of words, phrases, or sentences. Prepare the keys of the piano in the following way: A key somewhere in the middle of the keyboard is marked with the first letter of the chosen text. The next keys of the same color, alternating to left and right (or vice versa) are treated with the succeeding letters in the text; if a certain letter occurs a second time, it should be dropped, and instead the next letter which has not yet occurred taken, until every letter of the text is represented on the keyboard.

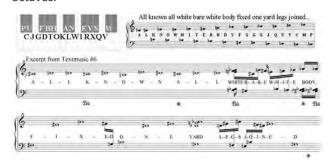
This procedure is then repeated with the keys of the other color, and then yet a third time, without taking the color of the keys into consideration.

The text can now be 'played' according to the three key-color-systems - and one can

- 1. play the letters singly, or together as syllables, words, phrases (in their order of appearance in the text) or even an entire sentence in all cases, the sound should be repeated as often as the number of syllables it contains,
- 2. change the position of the right pedal (between depressed and released), the loudness (between loud and soft), and the length of the

sound (between short and long) at best only at change of syllable, and the key-color at best only at change of word.

Figure 1 exemplifies of the application of these rules to the text *Ping* by Samuel Beckett, which begins with the words: "All known all white bare white body fixed one yard legs joined like sewn". The 25 different letters of the text ALKNOWHITEBRDYFXGSJQUVCMP (the only letter missing is Z) are assigned in turn to an equal number of black (pentatonic), white (diatonic) and mixed-color keys (chromatic). Figure 1 shows at top left and top right how these 25 letters are allocated chromatically, spanning exactly two octaves; the score's opening notes up to "joined" are also shown. In diatonic allocation, the 25 letters span 3½ octaves, in pentatonic allocation 5 octaves.



**Figure 1.** How the 25 different letters of Beckett's *Ping* are chromatically assigned to the keys of a piano according to the rules outlined in *Textmusic*. Also shown: the opening of *Textmusic Version 6*, based on the Beckett text.

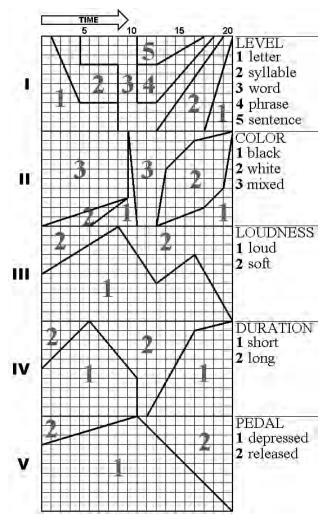
Soon after I drew up the rules of *Textmusic*, I realized that their algorithmic nature lent itself to incorporation

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into a computer program for the automatic generation of multiple versions of the piece, even following designs by persons other than myself. Indeed, of the 15 versions that were realized from 1971 to 1984, a computer program generated six, of which three were designed by others.

The program in question, written in 1971-72 in Fortran, was named *TXMS* (from *Textmusic*), its input first entered into an accompanying form chart, shown in Figure 2.



**Figure 2.** This chart shows fields for entering parameter values for computer-generating a version of *Textmusic*. The curves here are for *Version 4*, based on the text in the instructional verbal score itself.

TXMS is a stochastic program, generating notes according to probability values, previously entered as transitions into the chart shown above (here for Textmusic Version 4), from where the salient values are read and typed as input. Take e.g. the uppermost field for the distribution of letters, syllables, words, phrases and sentences. At the left, signifying the start of the

piece, the probability of single letters (level 1 or single notes) is 100%. One section later ( $^1/_{20}$ <sup>th</sup> of the piece, numbered above the chart in fives), the probability of syllables (level 2), initially at 0%, begins to increase, that of letters to decrease, until at the end of section 4 they respectively stand at 70% to 30%. At this point, the probability of words (level 3) is instantaneously set at 30%, that of syllables at 40%, that of letters remains fixed at 30%, values which remain in force till the end of section 8, where the probability of words jumps to 100% and stays there till the end of section 10. All through the process, random numbers — based on the respective probability — determine whether a single letter is to be converted to a note, or letters as part of a syllable, word, phrase or sentence to a chord.

The same system is used for the other parameters color, loudness, duration and pedal. For instance, at the start of the piece, the key-color is totally mixed (chromatic), a random half of the notes is loud and the other half soft, a random half of the notes is short and the other half long, and 70% of the events are played with the pedal depressed and 30% with it released.

Further information required by the chart, not shown here, are the number of hands, the number of fingers in each hand(!), the span of each hand measured in white keys, as well as the expected duration of the short events and that of the long ones.

There was a dearth of available notation programs in the early 1970s. I wrote my first one, XSC, with notes, replete with stems and beams, drawn on a plotter and directly readable by a performer, a bit later, from 1972-76 (the  $\ensuremath{\mathcal{H}}$  is a wildcard for the letters K, L and M in the three main modules "Keyboard reader", "Lister" and "Music writer", and the SC stands for "score"). TXMS's output was a kind of staff notation intended instead for regular line printers of the time, making it relatively easy to copy the music by hand from the output into a score. The characters used were []] for (vertical) staff lines and beams, [0] for note-heads, [-] for (horizontal) stems, [#] for sharps. By overprinting, I achieved results like those reconstructed and shown in Figure 3: an 8<sup>th</sup>-note D<sub>5</sub>sharp followed by a 16<sup>th</sup>-note D<sub>5</sub>-natural (every accidental applies to the note it precedes), as read from top to bottom in the treble clef.



**Figure 3.** A reconstructed example of the printed output *TXMS* with staff, note-heads, stems, beams and

#### **Autobusk**

## Harmonicity

In 1975, having left serialism far behind in my work, I became intrigued by the idea of regarding tonality and meter, eschewed by serialists, embraced by conservatives, as physical phenomena manifest as fields of variable strength: I worked towards music moving in a continuum ranging from atonal to tonal, from ametric to metric. To this end, in 1978 I found sufficiently satisfactory algebraic solutions, exemplified in the field of tonality by formulas for *numerical indigestibility* and *intervallic harmonicity* as shown in Figure 4 and as tables in Figure 5.

Formula for Indigestibility	Formula for Harmonicity				
$\xi(N) = 2\sum_{r=1}^{\infty} \left( \frac{n_r(p_r - 1)^2}{p_r} \right)$ whereby: $\sum_{r=1}^{\infty} p_r^{n_r}$	$\mathcal{H}(P,Q) = \frac{\operatorname{sgn}(\xi(Q) - \xi(P))}{\xi(P) + \xi(Q)}$				
2. N, n, p € natural numbers 3. p € prime numbers	whereby $sgn(x)=-1$ for $x<0$ , else $sgn(x)=+1$				

**Figure 4.** Formulas for the Indigestibility of a natural number and the Harmonicity of an interval ratio.

Indigestibility & of the natural									nicity 0.05
numbers 1-16	Interval	Prime Decomposition as Powers of							
20010 5 5 X 15 3	size (cts)	2	3	5	7	11	13	ratio	Harmonicit
	0.000	0	0	0	0	0	D	1:1	+00
	70.672	-3	-1	+2	0	0	0	24:25	+0.054152
N 5(N)	111.731	+4	-1	-1	0	0	0	15:16	-0.076531
1 0,000000	182.404	+1	-2	+1	0	0	0	9:10	+0.078534
2 1.000000	203.910	-3	+2	0	0	0	0	8:9	+0.120000
3 2.666667	231.174	+3	0	0	-1	0	0	7:8	-0.075269
4 2.000000	266.871	-1	-1	0	+1	0	0	6:7	+0.071672
	294.135	+5	-3	0	0	0	0	27:32	-0.076923
5 6.400000	315.641	+1	+1	-1	0	0	0	5:6	-0.099338
6 3.666667	386.314	-2	0	+1	0	0	0	4:5	+0.119048
7 10.285714	407,820	-6	+4	0	0	0	0	64:81	+0.060000
8 3.000000	427.373	+5	0	-2	0	0	0	25:32	-0.056180
9 5.333333	435.084	0	+2	0	-1	0	0	7:9	-0.064024
10 7.400000	470,781	-4	+1	0	+1	0	0	16:21	+0.058989
11 18,181818	498,045	+2	-1	0	0	0	0	3:4	-0.214286
12 4.666667	519.551	-2	+3	-1	0	0	0	20:27	-0.060976
13 22.153846	568.717	-1	-2	+2	0	0	0	18:25	+0.052265
14 11.285714	582.512	0	0	-1	+1	0	0	5:7	+0.059932
15 9.066667	590.224	-5	+2	+1	0	0	0	32:45	+0.059761
16 4.000000	609.776	+6	-2	-1	0	0	0	45:64	-0.056391
	617.488	+1	ō	+1	-1	0	ō	7:10	-0.056543
	680.449	+3	-3	+1	0	0	0	27:40	+0.057471
	701,955	-1	+1	0	0	0	ō	2:3	+0.272727
	729.219	+5	-1	o	-1	O	0	21:32	-0.055703
	764,916	+1	-2	ō	+1	0	0	9:14	+0,060172
	772.627	-4	0	+2	0	0	0	16:25	+0.059524
	792.180	+7	-4	0	0	0	0	81:128	
	813.686	+3	0	-1	0		0	5:8	-0.106383
	884.359	0	-1	+1	0	o	0	3:5	+0.110294
	905.865	-4	+3	0	0	0	0	16:27	+0.083333
		+2	+1	0	-1	0	0	7:12	
	933.129						-		-0.066879
	968,826	-2	0	0	+1	0	0	4:7	+0.081395
	996.090	+4	-2	0	0	0	0	9:16	-0.107143
	1017.596	0	+2	-1	0	0	0	5:9	-0.085227
	1088.269	-3	+1	+1	0	0	0	8:15	+0.082873
	1129.328	+4	+1	-2	0	0	0	25:48	-0.051370
	1137.039	-1	+3	0	-1	0	0	14:27	-0.051852
	1200 000	+1	0	0	n	0	0	1.2	+1 000000

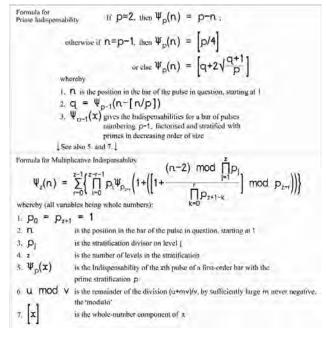
**Figure 5.** Tables for the Indigestibility of a natural number and the Harmonicity of an interval ratio.

Based on an algebraic evaluation of a quality of natural numbers based on their size and divisibility, which I call *indigestibility* (whereby small primes and their products are more 'digestible' than products containing larger primes), the formula for the *harmonicity* of an interval ratio yields values such as +1.0 for the 1:2 octave, +0.273 for the 2:3 perfect 5<sup>th</sup>, -0.214 for the 3:4 perfect 4<sup>th</sup> (the negative sign indicates a polarity to the upper note, here the *root* of the interval; a positive polarity signifies a lower-pitched root), and +0.119 for the major 3<sup>rd</sup> 4:5 etc., as seen in Figure 5.

With these formulas it was found possible to rationalize scales known by interval size, e.g. the chromatic scale given as multiples of 100 cents was rationalized to the values

1:1 15:16 8:9 5:6 4:5 45:32 2:3 5:8 3:5 5:9 8:15 1:2, a solution that has been known and accepted for centuries. Any pitch-set known in terms of cents can be similarly rationalized by the harmonicity algorithms described above.

Moving on to meter, another set of formulas governs the metric properties of the music I set out to compose, shown in Figure 6. Terms I have introduced will next be explained (the most important of which are *Stratification* and *Metric Indispensability*), along with terms of general usage.



**Figure 6.** Formulas for Metric Indispensability of pulses in Prime and in Multiplicative Meters.

A meter is *prime*, i.e. containing a prime number of equal time-units (here called *pulses*) e.g. 2, 3, 5, 7, 11, etc., or

multiplicative, i.e. containing as pulse quantity a product of primes, e.g. 4, 6, 8, 9, 10, etc. Additive meters (e.g. 3+3+2 pulses = 8) are not covered here. Meters exhibit a certain stratification, e.g. that shown in Figure 7 at left. A meter of 12 pulses, for instance, can be broken up in three ways, into 3 groups of 2 groups of 2, i.e. 3x2x2, or instead

or 2x2x3. This last stratification is seen in Figure 7: the first metric level contains one note or time-unit, the second level two units, the third 4 and the fourth 12. Time-units on the top two metric levels can be called *beats*, on lower levels, *pulses*, though the longer a prime meter, the less relevant the beat/pulse distinction — in this paper, 'pulse' is used for both. Prime meters have one-level stratifications.

Stratification example	Rhythmic Dilution						
12 = J.	meter:	3 4	6 8				
16 <sup>-</sup> 0.	pulses; indisp.:	123456 503142	123456 502413				
-1 1	6	ллл					
	5	AJJ	AMI				
× 2	4	小小刀	1,11,1				
= J. J. J. J.	3	444	ふっふか				
× 3	2	1 3	1, 1,				
= ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	1	1,2 2	1772.				

Figure 7. Examples of Stratification and Rhythmic Dilution.

That said, I now outline the method to evaluate the relative metric relevance of any pulse in a prime or multistratified meter, called its *Metric Indispensability*, calculable by the formulas in Figure 6 (not explained here). Point of departure is the *Prime Indispensability* for prime meters (e.g. 1-0 for a 2-pulse meter, 2-0-1 for a 3-pulse meter,

4-0-3-1-2 for a 5-pulse meter etc., given by  $\Psi$ , upper-case psi, in Figure 6, top). Next in line is *Multiplicative Indispensability* (see  $\psi$ , lower-case psi, in Figure 6, bottom), derived respectively from the indispensabilities of the component prime meters' pulses. The higher the indispensability, the more relevant the pulse for maintaining the meter.

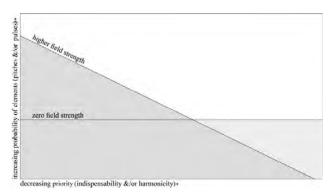
A 6-pulse meter as 3x2 (e.g. 3/4) has the indispensabilities 5-0-3-1-4-2, a 6-pulse meter as 2x3

(e.g. 6/8) 5-0-2-4-1-3. Figure 7 shows at right a system of *rhythmic dilution* for illustrating indispensability. Removing attacks in order of increasing indispensability starting with 0, one sees that the corresponding notated rhythms preserve the metric feel all the way through, in 3/4 as well as in 6/8.

The Intervallic Harmonicity and Metric Indispensability formulas – along with several other relevant algorithms – were incorporated into the real-time program *Autobusk*, which I wrote in Pascal between 1986 and 2000 (from 1987 on an Atari ST computer). Two important auxiliary modules are *HRM* (for Harmonic Rationalization Measures), for the compilation of scales – entered as cent values – into lists of scale-degree harmonicities, and *IDP* (for Indispensability Determination Program) for the compilation of meters – entered as stratification – into pulse indispensability lists.

Autobusk is a stochastic program. It generates timeconcurrent streams of controlled random rhythmicized MIDI notes based on probabilities calculated from the Harmonicity and Indispensability formulas in the light of a fundamental consideration - at zero tonal fieldstrength (for atonal music), all pitches of the scale(s) being used are equally probable, a property shared by the twelve-tone technique; at zero metric field-strength (for ametric music), all pulses of the meter(s) being used are equally probable in whether they are attacked or not. But for a high field-strength, the probability of pitches of higher tonic-related harmonicity and the probability of attack on pulses of higher indispensability are raised, those of pitches/pulses of lower harmonicity/ indispensability are lowered. Collectively regarding pitches/pulses as elements, one can state that tonal/metric field strength is proportional to the gradient of a straight line marking element probability on the yaxis as against dimensionally contextual priority (harmonicity/indispensability) on the x-axis - see Figure 8. Changing the gradient results in a change in fieldstrength.

In addition to the priority-probability gradient, a further mechanism was applied, *inter-temporal coordination*, locking the micro-temporal (pitch) to the macro-temporal (pulse): the tonality degree is thereby varied according to indispensability — strong pulses have (for non-zero-field-strength) pitches more harmonic than those on weak pulses. This allows for Schenker's structural and prolonging tones on strong and weak pulses, respectively.



**Figure 8.** A straight line showing probability as a function of priority, the gradient as a function of field-strength.

Autobusk receives as input a list of scales and meters (pre-compiled by HRM and IDP, extensions .HRM and .IDP), and most likely a parameter score (extension .PRK) containing time-tagged values for 12 parameters, seen accordingly numbered in the screen shot in Figure 9: "metriclarity" and "harmoniclarity" mean the metric and tonal field-strength. If the event of the absence of a .PRK file, user-defined preset (or else default) parameter values are used.

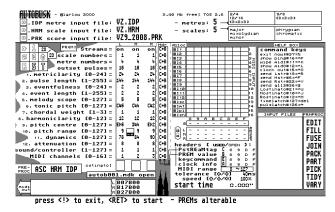


Figure 9. Screen-shot of Autobusk.

Parameters can be changed in real-time by key-typing, the mouse, a MIDI input device such as a keyboard and/or time-tagged instructions in a .PRK file. The output, usually MIDI notes, is sent to the MIDI port and/or to a file. The program is freely downloadable at Mainz University <a href="http://www.musikwissenschaft.uni-mainz.de/Autobusk/">http://www.musikwissenschaft.uni-mainz.de/Autobusk/</a>, ready to be run on an Atari, should one have one, together with a pdf user manual. In order to run it in Windows, one needs an Atari emulator, as indicated by the site. For use on a Macintosh, an additional Windows emulator is necessary.

# Synthrumentator

In 1981, while planning a new work for chamber ensemble, I had the idea of writing a spectral piece in which the overall sound of the ensemble would reflect the sounds of speech. For this I would convert a spectral analysis of spoken words into a playable score for nearly pure tones, e.g. string harmonics. Playing the score engenders the synthesis of harmonic spectra, for which the best phoneme types are vowels, approximants, laterals and nasals (thus excluding plosives, fricatives and trills).

For the envisaged composition, I put together nine nonsensical but grammatically correct German sentences based on words consisting solely of these harmonically synthesizable phonemes - of the languages I was familiar with at that time, German seemed especially suitable due to its systematic phonetic spelling as an aid in looking for usable words. These sentences – the title of the piece, *Im Januar am NiI*, was taken from one of them – were Fourier-analyzed and the results converted into something like a MIDI file (this work predated MIDI by three years): every set of six Fourier time-windows was merged into an chord consisting of overtones, each with its pertinent amplitude, as later with pitch and velocity in a MIDI file.

The really significant follow-up to this procedure was the subsequent re-setting of all amplitudes to multiples of an arbitrary amplitude, termed the *amplitude tolerance*: any partial in one chord having the same altered amplitude as the identical partial in the following chord is sonically connected to that partial, i.e. it is not repeated but held. More on this procedure – termed *calming* – later.

Figure 10 shows (above) the words in Armenien scored for bass clarinet playing the fundamental and for seven strings playing the partials and (below) a graphic representation of the same, which strongly resembles the sonagram of the spoken words. I called this technique Synthrumentation, from "synthesis by instrumentation". From 1981 till the completion of the piece in 1982 and that of its final revised version in 1984, I wrote all the software, from the Fourier analysis to the generation of the score, a total of twenty programs in Fortran. The output was printed using my notation program <code>XSC</code>, mentioned above, on a 9-pin dot-matrix printer.



**Figure 10.** Synthrumentation of the words *in Armenien* in the chamber ensemble piece *Im Januar am Nil*: compact score (above) and graphic representation of the score (below).

In the course of the years, I used synthrumentation for a number of pieces, prompting me to combine all modules into a single Linux GNU Pascal program for repeated use named Synthumentator. In principle, the procedure is the same: a Fourier analysis of a sound wave is converted to a MIDI file of chords comprising partials of the fundamental analysis frequency (my favorite: 49 Hz, almost exactly  $G_2$ , and a whole-number subdivision of the sampling rate 44,100 Hz). This conversion maps frequencies to MIDI notes, maps amplitudes to velocity.

Finally the MIDI file is calmed. For instance, with a tolerance (now called *velocity tolerance*) of 4, all velocities are re-set to multiples of 4, i.e. 0, 4, 8, 12 etc. Notes now with velocity 0 are removed. If a particular note in any one chord, say  $G_4$ , has the same adjusted velocity, say 64, as the  $G_4$  in the next chord, the note-off of the first chord and the note-on of the second are removed, lengthening the former. The higher the velocity tolerance, the smaller and sparser the resulting output file. A low velocity tolerance will result in a dense output file, perhaps obscuring the desired timbral link to the sound source. The main task in using this program is to find the optimal velocity tolerance.

The program is being currently rewritten in C for Mac OS and Windows.

#### ...or a cherish'd bard...

In 1998 I decided to write a solo piece for the pianist Deborah Richards in order to commemorate her 50<sup>th</sup> birthday. A common means of honoring a person in a music score is to take those letters of the person's name which are available as note names (i.e. A-G in English, with the additional H and S in German) and to use these notes repeatedly. In fortunate cases like ABEGG and BACH, the complete names are available as notes. However, before discarding the idea of using Ms Richards' name in this way, I noticed that in her first name, the letters DEB and AH were definitely usable as notes in German, and that the intervening letters OR denote a logical operation. Further, DEB belong to a whole-tone scale (B is German for B-flat) and AH (H is German for B-natural) belong to the other whole-tone scale. Finally I also noticed that the letters DEB and A are digits in the hexadecimal number system.

I accordingly set up two pitch-chains in the two wholetone scales, one chaining transpositions of DEB and the other transpositions of AH — see Figure 11 (top). In theory, each chain moves in pitch and time to and from ±infinity. Next I converted the hex numbers DEB and A to their binary equivalents 1101 1110 1011 and 1010. These became the repeatable rhythmic cycles in Figure 11 (center): 1 = attack, 0 = silence — the H in AH, not a number, was added as a silence 0000. Combining the pitch chains and the rhythms, I obtained the rhythmicized pitch chains shown in Figure 11 (bottom).



Figure 11. Pitch chains, rhythmic cycles and both based on DEB and AH.

After this I set up 120 DEB and, separately, 120 AH rhythmic chains successively and parallel to each other, such that all transections of  $D_4$  (Middle D) are time-equidistant at intervals of four seconds, i.e. on the first beat of every bar from 1 to 120.

Figure 12 shows an example of this procedure as applied to the infinite DEB chain. The x-axis marks the 120 bars of the piece, the y-axis a range of 40 octaves from 0.28  $\mu\text{Hz}$  to 308 MHz (!). The middle horizontal line marks  $D_4$  at 293.67 Hz. Instead of crossing this line every bar, as in the piece, this graph shows for reasons of space a crossing every 10 bars. The basic DEB motif, both in pitch and rhythm, is displayed in a small box at upper left – the entire graph consists of chains of this motif, reduced to 50% in size.

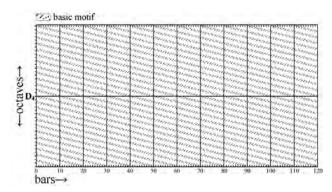
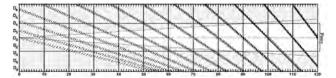


Figure 12. Parallel DEB chains crossing  $D_4$  downwards every ten bars (in the piece this happens every bar).

To change this static scenario into a dynamic one, I then made the gradient of the chains successively increase with time, forming primordial DEB and AH scores.

Next followed the containment of the piece within a triangular pitch filter, starting at the beginning (left) at a width of zero half-steps centered on D<sub>4</sub>, gradually expanding, the width at any bar in half-steps equalling the bar number, reaching a range of 10 octaves at bar 120 (right). Obviously the range transcends that of the piano at around bar 88; the printed score nonetheless contains notes extending beyond. The result for the DEB score is displayed as a graph in Figure 13.



**Figure 13.** The DEB score with increasing chain gradients and triangular pitch filter.

The final step was a transition in time from the filtered DEB score to the filtered AH score by means of random selection – at the start of the piece, the choice of a note from the DEB score is 100% probable, that of a note from the AH score 0%. At the end, the probabilities are reversed, so that in the middle, at bar 60, both scores are subjected to a 50% probability each. Thus every note of

the piece is taken either from the DEB score or from the AH score:

DEB OR AH, moving from the former to the latter. As a consequence, the music of the opening bars is in the whole-tone scale containing DEB, that in bar 60 is highly chromatic with all twelve notes in every octave, and the final notes are in the other whole-tone scale containing AH. The whole composition was made by once-used software.

Due to the rising gradients, the resulting durational values were of an irrational nature. I rationalized the score with my program *Tupletizer*, converting irrational time-values to notatable tuplets by rounding within flexible constraints and with controllable error. Figure 14 shows bars 92-94 as notated in *Sibelius*: the diamond-shaped and crossed note-heads are an octave higher/lower than written, the former still within the piano range and the latter beyond.



Figure 14. An excerpt from the Sibelius-printed score.

The title "...or a cherish'd bard..." is an anagram of the name Deborah Richards. Here is the dedication:

Full fifty years, the most whereof well spent / In service of the Muse, wherefore I pray / That Lady Fortune add three score and ten. / Yet I, a clown cerebral\*, so some say, / Unfit in words, resort to music's way / To help submit my prayer in this regard — / Meseems a minstrel, or a cherish'd bard / Would better wield in verse his worthy pen.

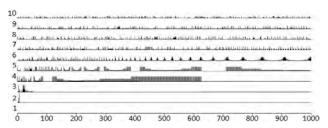
\*an anagram of the name Clarence Barlow

# **Approximating Pi**

In 2007 my attention was drawn by my colleague Curtis Roads to the series  $\pi = 4(1-\frac{1}{3}+\frac{1}{5}-\frac{1}{7}+\frac{1}{9}\cdots)$ , something I had not thought about since my school days. Almost immediately, an electronic music installation began to shape in my mind, in which the amplitudes of ten partials of a complex tone would reflect the first ten digits of the progressive stages of convergence — with each added component of the series — toward the final value. In May 2008, the installation, *Approximating Pi*, which I realized wholly in Linux GNU Pascal, was given its premiere.

For each convergence, I decided on a time frame of 5040 samples, i.e. 8¾ frames per second. All time frames contain a set of ten partials of an overtone series, multiples of the frequency 8¾ Hz, which automatically results from the width of the frame, 5040 samples. The reason for this number of samples is that is can be neatly divided into 2 to 10 exactly equal segments, corresponding to the partials (half this value, 2520, which as least common multiple of the numbers 1-10 is amenable to the same, corresponds to 17½ frames per second, too fast for my purposes).

The partials are square waves of amplitude 2 raised to the power of the n<sup>th</sup> digit in the decimal representation of the convergence. In the case 3.14159..., for instance, the amplitudes of the ten partials are  $2^3$ ,  $2^1$ ,  $2^4$ ,  $2^1$ ,  $2^5$ ,  $2^9$  etc. The amplitudes are then rescaled by a multiplication by the arbitrary factor  $2^{\pi}/_n$ , forming the envelope of a sawtooth spectrum, where 'n' is still the partial number.



**Figure 15**. The digits of the first 1000 approximations of  $\pi$ , shown to the tenth digit, as amplitudes of a 10-partial spectrum.

Figure 15 graphically displays 1000 convergences (x-axis) and the corresponding amplitudes of the ten digits (y-axis). See the prominent bulges caused by the digit 9 in  $6^{th}$  place.

Since successive convergences cause the digits to settle down from left to right to a value gradually approaching that of  $\pi$ , one can expect the resultant timbre to move from initial turbulence to a final near-constancy, which it

does. As an example, with four digits, the series goes from an initial 4.000 through 2.667, 3.467, 2.895, 3.340, 2.976 to 3.284. At this 7<sup>th</sup> convergence, the first digit stabilizes at the value 3. The second digit similarly stabilizes at the value 1 at the 25<sup>th</sup> convergence, the third digit at the value 4 at the 627<sup>th</sup> (these three are visible in Figure 15), the fourth at the value 1 at the 2454<sup>th</sup> convergence. With ten digits it would take 2,425,805,904 convergences before the final digit stabilizes and real constancy is attained. At a rate of 8¾ convergences per second, this would take 8¾ years.

There is no need for one to wait that long, however. The installation can be pitch-transposed and thus shortened by regular sample dropping; it can also be time-truncated. In a frequently presented version, eight sound channels contain transpositions from the original 8% Hz to values 9, 28, 50, 72, 96, 123, 149 and 175 times higher (from channel two close to the arbitrary series  $9\pi^{(1+\frac{1}{2}+\frac{1}{2}+\frac{1}{2})}$ , where  $\chi$  is the channel number plus one). Versions of various durations - 5, 8, 15 and 76 minutes - and audio configurations - 2, 5 and 8 channels - have been realized. In the 8-minute version (more exactly  $7'37^1/_7"$ ), the duration was truncated to 36,000 convergences for the lowest transposition; the highest transposition reaches the 700,000 th convergence, at which point the first six digits are already stable.

#### Conclusion

Algorithms are a means to an end. Their elegance is no guarantee of musicality. In the case of the examples above, algorithms were shaped by an anticipated musical result, in the end often containing intriguing aspects, creating a new aesthetic. This after scrutiny was either welcomed... or rejected, leading to a revision of the algorithm.

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# [Abstract in Korean | 국문 요약] 나의 작품을 통해 살펴 본 알고리듬적 작곡: 1971년부터 2008년 동안 쓰여진 작품을 중심으로

클라렌스 발로

1971년, 14년 간의 즉흥 작곡 방식을 바꾸면서, 그 뒤로 나는 사실상 주로 알고리듬에 근거한 작품들을 썼다. 그중 일부는 하나의 알고리듬을 여러 번 사용하여 만들어졌고 그 결과물의 속성과 특징은 입력물로부터 비롯되었다. 반면, 한편의 작품만을 만들어 낼 목적으로 알고리듬을 한 번만 사용한 경우도 있다. 아울러, 언어적 지시 사항으로부터 복잡한컴퓨터 프로그램에 이르는 알고리듬이 작곡 과정에 사용되었다.

1971년부터 작곡한 80여개의 작품 중 약 4분의 1은 언어로 된 악보 세 개를 이용해 작곡하였다. 그중《Textmusic》은 쓰여진 글을 음으로 바꾸는 방식이고, 《...until...》은 음정 관계에 따라 조직적으로 작동하며, 《Relationship》은 화성과 박자의 맥락 안에서 선율과 장단의 복잡한 정도에 따라 작동한다. 다른 4분의 1에 해당하는 작품은 독립적인 컴퓨터 프로그램 세 가지를 이용해 작곡하였다. 그중 《TXMS》는 《Textmusic》을 소프트웨어화한 것이고, 《Autobusk》는 음계와 박자 아울러 조성의 박절과 같은 12개의 실시간 매개 변수를 사용하는 연속적인 미디 음들을 생성한다. 아울러 《PAPAGEI》는 즉흥 연주자와의 실시간 상호 연주를 바탕으로 미디 이벤트를 생성한다. 하지만, 또 다른 4분의 1은 한편의 작품을 위해 한 개의 알고리듬만을 사용하였다. 《Synthrumentator》와 말소리를 악기를 위한 악보로 변환하기 위한 《Spectasizer》와 같은 컴퓨터 프로그램의 경우 작품의 일부만을 위해 사용하기도 하였다.

이 글에서 필자는 《TXMS》, 《Autobusk》와 《Synthrumentator》에 대해 설명할 것이며, 아울러 전용 소프트웨어를 이용해 작곡한 작품 두 편 《…or a cherish'd bard…》와 《Approximating Pi》를 소개한다. 전자의 경우 알고리듬이 음높이와 장단, 형식 등 모든 음악적 변수를 생성해내고 후자의 경우 대수적으로 정의된 알고리듬이 소리의 파형을 생성해낸다.